

1.5 COMPLEX SOLUTIONS TO THE QUADRATIC EQUATION

$$ax^2 + bx + c = 0$$

DISCRIMINANT

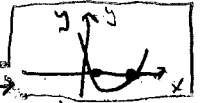
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$D = b^2 - 4ac > 0$$

$$D = b^2 - 4ac = 0$$

$$D = b^2 - 4ac < 0$$

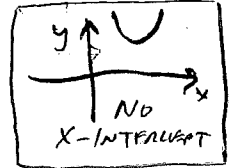
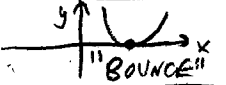
GRAPHICALLY.

2. Real Solutions
= X-INTERCEPTS1. Real Solution
REPEATED TWICE

2. Complex Solution



CONJUGATE PAIRS!



Ex. $x^2 + 4 = 0$

$$x = \pm \sqrt{-4}$$

$$x = \pm 2i \quad x = 2i, x = -2i$$

Ex. $3x^2 - 2x + 5 = 0$

$$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(3)(5)}}{2(3)}$$

$$\frac{2 \pm \sqrt{4 - 60}}{6}$$

$$= \frac{1}{3} \pm \frac{\sqrt{-56}}{6} = \frac{1}{3} \pm \frac{\sqrt{14}i}{3}$$

$$\left\{ \begin{array}{l} \frac{1}{3} + \frac{\sqrt{14}i}{3} \\ \frac{1}{3} - \frac{\sqrt{14}i}{3} \end{array} \right.$$

$$\sqrt{56} = \sqrt{4 \cdot 14} = 2\sqrt{14}$$

$$\frac{\sqrt{-56}}{6} = \frac{2\sqrt{14}i}{3}$$